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# WAVES

1 OMQ+1 VSAQ + 1 SAQ [1M+2M + 4M = 7M]

## CONCEPTS & DEFINITIONS

1. A **wave** represents a disturbance that moves in a medium or space.
2. Vibrations of particles produce **Mechanical waves** and they require a medium to propagate.
3. The changes in electric field in space produce **Electromagnetic waves** and they do not require any medium to propagate.
4. Waves in which the particles of the medium vibrate in perpendicular to the direction of wave propagation are called **transverse waves**.
5. Waves in which the particles of the medium vibrate along the direction of wave propagation are called **longitudinal waves**.
6.  $y = A \sin(kx - \omega t + \phi)$  represents a progressive wave along +ve x-direction.
7.  $y = A \sin(kx + \omega t + \phi)$  represents a progressive wave along -ve x-direction.
8. Amplitude  $A = y_{\max}$
9. Angular wave number  $k = \frac{2\pi}{\lambda}$  where  $\lambda$  is wavelength.
10. Angular frequency  $\omega = 2\pi\nu$
11. Phase gives the position and direction of motion of the particle in wave motion.
12. Distance between two successive points of same phase is called **wavelength ( $\lambda$ )**.
13. Phase difference between two points separated by one wavelength is  $2\pi$  radians.
14. Phase difference between two points  $\Delta\phi$  separated by distance  $\Delta x$  is given by  $\Delta\phi = \frac{2\pi}{\lambda}(\Delta x)$
15. The number of waves per second or number of oscillations per second is called **frequency ( $\nu$ )**.
16. The time taken by a particle in wave motion to complete one oscillation is called **period (T)**.
17. Relation between frequency & period  $\nu = \frac{1}{T}$
18. Speed of a progressive wave  $V = \nu\lambda$  (or)  $V = \frac{\lambda}{T}$  (or)  $V = \frac{\omega}{k}$
19. Speed of transverse wave in a stretched string  $V = \sqrt{\frac{T}{\mu}}$  where  $T$  = tension and  $\mu$  = linear density.

20. Mass per unit length is linear density. Linear density of a string  $\mu = \frac{M}{L} = \frac{m}{l}$  or  $\mu = A\rho = \pi r^2\rho$  where A is area of cross section of the given wire, r is its radius and  $\rho$  is density.
21. Speed of longitudinal wave in a liquid  $V = \sqrt{\frac{B}{\rho}}$  where B = Bulk modulus of given liquid and  $\rho$  = density of liquid
22. Speed of longitudinal wave in a solid  $V = \sqrt{\frac{Y}{\rho}}$  where Y = Young's modulus of given solid  $\rho$  = density of solid
23. According to Laplace speed of longitudinal wave in a gas  $V = \sqrt{\frac{\gamma P}{\rho}}$  where P = pressure,  $\rho$  = density and  $\gamma$  = ratio between specific heats (specific ratio)
24. Principle of superposition  $\vec{y} = \vec{y}_1 + \vec{y}_2 + \vec{y}_3 + \dots$
25. A wave reflects at closed end with a phase difference of  $\pi$  radians ( $180^\circ$ ).
26. A wave reflects at open end with same phase. (i.e.,  $2\pi$  radians or  $360^\circ$ ).
27. The resultant wave formed due to superposition of two progressive waves travelling in opposite directions is called standing or **stationary wave**.
28. Amplitude at node  $A_N = A_1 - A_2$
29. Amplitude at antinode  $A_{AN} = A_1 + A_2$
30. Always nodes are formed at closed ends (rigid boundaries).
31. Always antinodes are formed at open ends (free boundaries).
32. Distance between two successive nodes or antinodes is  $\frac{\lambda}{2}$ .
33. Distance between a node and its adjacent antinode is  $\frac{\lambda}{4}$ .
34. When a **stretched string** is vibrating in fundamental mode, length of the string  $l = \frac{\lambda}{2}$   
 fundamental frequency (first harmonic)  $v_1 = \frac{V}{2l}$  or  $v_1 = \frac{1}{2l} \sqrt{\frac{T}{\mu}}$   
 xth harmonic frequency  $v_x = xv_1 = \frac{x}{2l} \sqrt{\frac{T}{\mu}}$  where,  $x = 1, 2, 3, \dots$
35. When an **open pipe** is in fundamental mode of vibration, length of the open pipe  $l = \frac{\lambda}{2}$   
 fundamental frequency  $v_1 = \frac{V}{2l}$   
 xth harmonic frequency  $v_x = xv_1$  where,  $x = 1, 2, 3, \dots$

36. When a **closed pipe** is in fundamental mode of vibration, length of the closed pipe  $l = \frac{\lambda}{4}$

fundamental frequency  $\nu_1 = \frac{v}{4l}$

$x^{\text{th}}$  harmonic frequency  $\nu_x = (2x - 1)\nu_1$  where,  $x = 1, 2, 3, \dots$

37. The phenomenon in which waxing and waning of sound at regular intervals is heard is called **beats**.

Number of beats/second is called beat frequency.

$$\nu_{\text{beat}} = \nu_1 \sim \nu_2$$

The time interval between two successive beats is called beat period. Beat period  $T = \frac{1}{\nu_1 \sim \nu_2}$

38. If a tuning fork is loaded with wax, its frequency decreases.

39. If a tuning fork is filed, its frequency increases.