

5. PERMUTATIONS & COMBINATIONS

$(2 \times 2) + (2 \times 4) = 12$ Marks

IMP FORMULAS, KEY CONCEPTS

- 1) **Fundamental Principle of counting:** If an operation A can be performed in m ways and another operation B, which is independent of A can be performed in n ways, then both the operations A and B can be performed in $m \cdot n$ ways
- 2) **Fundamental principle of Addition:** If a work A can be done in m ways, another work B which is independent of A, can be done in n ways, then the number of ways that, atleast one of A, B (i.e., A or B) can be done is $(m+n)$.
- 3) The number of permutations of n dissimilar things taken r at a time is

$${}^n P_r = \frac{n!}{(n-r)!} = n(n-1)(n-2)\dots(n-r+1) = \text{product of } r \text{ consecutive integers starting from } n$$
 = number of one one function that can be defined from A to B, where $O(A)=n$, $O(B)=r$
- 4.1) The number of permutations of 'n' dissimilar things taken r at a time, when repetition of things is allowed any number of times is n^r .
- 4.2) The number of permutations of n dissimilar things taken r at a time with **at least** one repetition is $n^r - {}^n P_r$.
- 4.3) The number of functions that can be defined from a set containing m elements into a set containing n elements is n^m .
- 5) The number of linear permutations of 'n' things, in which there are p alike things of one kind, q alike things of the 2nd kind, r alike things of the 3rd kind and the rest are different is $\frac{n!}{p!q!r!}$
- 6) The number of circular permutations of 'n' dissimilar things taken all at a time is $(n-1)!$.
- 7) The number of circular permutations of n things, when orientation of things is not considered, is $\frac{(n-1)!}{2}$ (half of the actual number of circular permutations).
- 8) The number of combinations of 'n' dissimilar things taken 'r' at a time is ${}^n C_r = \frac{n!}{(n-r)!r!} = \frac{{}^n P_r}{r!}$
- 9.1) ${}^n C_r = {}^n C_{n-r}$
- 9.2) ${}^n C_r + {}^n C_{r-1} = {}^{(n+1)} C_r$
- 9.3) If ${}^n C_r = {}^n C_s$ then $r = s$ or $r+s = n$
- 10) The number of diagonals in a regular polygon of n sides is $\frac{n(n-3)}{2}$
- 11) The number of selections of (p+q) things taken (i) any number (0 to p+q) at a time when p things are alike of one kind and q things are alike of other kind = $(p+1)(q+1)$ (ii) one or more at a time (i.e., atleast one at a time) = $(p+1)(q+1) - 1$.
- 12) If m, n are distinct positive integers, then the number of ways of dividing 'm+n' things into two groups containing 'm' things and 'n' things respectively is $\frac{(m+n)!}{m!n!}$